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**Bragg Cell on  $\text{TeO}_2$  for 2-D Deflector with  
Reduced Drive Power: Analysis, Design,  
and Experimental Examination**



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## TABLE OF CONTENTS

<b><u>SECTION</u></b>	<b><u>TITLE</u></b>	<b><u>PAGE</u></b>
1.0	Abstract.....	1
2.0	Introduction.....	1
3.0	Analysis of the Deflector Frequency Characteristic.....	2
4.0	Optimal Deflector Design.....	10
5.0	Experimental Investigations of the 5.5° Deflector.....	12
6.0	Discussion of Results.....	16
7.0	Conclusions.....	17
	References.....	21
	Figures.....	23

## LIST OF FIGURES

<b><u>FIGURE</u></b>	<b><u>CAPTION</u></b>	<b><u>PAGE</u></b>
Fig. 1.	The vector diagram illustrating acousto-optical interaction of the plane light wave with divergent sound beam in $\text{TeO}_2$ .....	23
Fig. 2.	Typical frequency characteristic of $\text{TeO}_2$ deflector.....	24
Fig. 3.	Frequency characteristics of the $6^\circ$ deflector at different $P_a$ .....	25
Fig. 4.	Bifurcation (curve 1) and narrowing (curve 2) of frequency characteristic.....	26
Fig. 5.	Frequency characteristics of the $6^\circ$ deflector at different constructive parameters.....	27
Fig. 6.	Frequency characteristics of the $5.5^\circ$ deflector at different wavelength.....	28
Fig. 7	Experimental setup for measuring frequency dependence of deflected light intensity.....	29
Fig. 8.	Construction of Bragg cell for 2-D deflector.....	30
Fig. 9	Frequency dependencies of the input $VSWR$ of the $5.5^\circ$ deflector with an optimal matching network (1 - calculated, 2 - measured).....	31
Fig. 10	Dependence of the $5.5^\circ$ deflector frequency characteristic on the adjustment angle $\theta_{adj}$ .....	32
Fig. 11	Dependence of the $5.5^\circ$ deflector frequency characteristic on the drive power $P_{dr}$ . $\theta_{adj} = \theta_{adj0}$ ; $P_{dr} = 200$ mW (1); $P_{dr} = 400$ mW (2); $P_{dr} = 600$ mW (3).....	33
Fig. 12	Dependence of the $7.9^\circ$ deflector frequency characteristic on the drive power $P_{dr}$ . $P_{dr} = 800$ mW (1); $P_{dr} = 400$ mW (2).....	34
Fig. 13	Normalized intensity vs frequency of light diffracted under Bragg angle at different constructive parameters and drive power.....	35
Fig. A1.	The diagram for calculating of the numerical functions $\alpha_c(\theta_1)$ and $f_c(\theta_1)$ and $\alpha(f)$ .....	36

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## 1.0 Abstract

The frequency characteristic dependence on acoustic power and the constructive parameters of a non-axial Bragg cell have been analyzed using numerical simulations. The numerical results suggest an explanation of the rectangular frequency form, which has been observed by other researchers in experiment when the incident angle is slightly different from the calculated one. Bragg cells with incident angles of  $5.5^\circ$  and  $6^\circ$  were studied. Theoretically, drive power can be reduced by increasing the length of interaction and lowering the operating frequency. 1-D Bragg cell for 2-D construction with crossed cells was fabricated and the theoretical effects were confirmed experimentally. Drive power for the  $5.5^\circ$  Bragg cell was half as large as the  $7.9^\circ$  Bragg cell; however, its bandwidth was only 27.1 MHz instead of the expected 40 MHz due to a transducer bandwidth limitation.

## 2.0 Introduction

Acousto-optic (AO) Bragg cells on  $\text{TeO}_2$  are widely used in practice. They are especially useful in 2-D deflector with crossed cells because of their fabrication simplicity. But in this case drive power  $P_{dr}$  grows significantly because of the decreased  $L/H$  ratio (Here  $L$  and  $H$  are length and height of the acousto-optic interaction ("AOF") domain). It is important therefore to study ways of reducing drive power. There are already a considerable number of papers dealing with the

midband degeneracy (non-axial deflector) was proposed<sup>2</sup>, to 1984 there were no attempts to solve any optimization problems for it. Then a set of papers was published<sup>6-9</sup> within which these problems were studied, but the results were only appropriate for deflectors with efficiency less than 0.5. Besides, there were no experimental data in those works. Some experimental results concerning the drive power of the 6° deflector were presented in<sup>2,4,10</sup>; however, there were no grounds in these papers why exactly the 6° interaction was chosen without considering optimization. Recently works appeared<sup>11,12</sup> in which other non-axial deflectors (8°, 9°, 10°) were studied theoretically and experimentally, but they did not specify any data about the drive power.

The objectives of this work are to clarify limiting factors for design of non-axial deflector on TeO<sub>2</sub> with reduced drive power, and experimentally verify the optimum design results in the fabrication of a cell for 2-D deflector with crossed cells.

Our investigations are based on a simple and well known fact that diffraction efficiency improves when either the interaction length  $L$ , (or the piezoelectric transducer length) increases (see Fig. 1). Thus, it is possible to decrease  $P_{dr}$  increasing  $L$ .

### **Analysis of the deflector frequency characteristic**

In order to establish the design limitations for when  $L$  is increased, it is necessary to evaluate what happens from this procedure. First, the AOI bandwidth decreases due to reduced sound beam divergence. It is possible to eliminate the effect by lowering an operating frequency, but then we need to take into account other factors which are dependent on frequency in different ways; e.g., polarization of incident light and acoustic loss. In this case acoustic loss only decreases causing increased efficiency, but the incident light ellipticity increases causing reduced efficiency.

Therefore it seems reasonable to lower the operating frequency until the bandwidth stays greater than some given value. We shall analyze the deflector frequency characteristic to clarify

the basic factors that it depends on.

A vector diagram of AOI is shown in Fig. 1. Here curves  $|k_1(\theta)|$  and  $|k_2(\theta)|$  are cross-sections of the light wave vector surfaces by the  $(\bar{1}\bar{1}0)$  plane,  $\theta$  is an angle between the  $[001]$  axis and an arbitrary light vector  $\mathbf{k}$ . The divergent sound wave is represented by a set of wave vectors  $\mathbf{K}(\alpha)$ , e.g.,  $\mathbf{K}_B$ ,  $\mathbf{K}_{N1}$ ,  $\mathbf{K}_C$ ,  $\mathbf{K}_{N2}$ ,  $\mathbf{K}_D$ , where  $\alpha$  is the angle between the  $[110]$  axis and an arbitrary vector  $\mathbf{K}$ . Efficient AOI occurs when the Bragg conditions are satisfied, i.e., vectors  $\mathbf{k}_1(\theta_1)$ ,  $\mathbf{k}_2(\theta_2)$  and  $\mathbf{K}(\alpha)$  are closed as it is shown in Fig. 1 for the ABO triangle. The frequency characteristic is formed as a result of the incident light wave vector  $\mathbf{k}_1(\theta_1)$  interaction with a set of the sound wave vectors  $\mathbf{K}(\alpha)$ . Thus, its shape is obviously dependent on the incident angle  $\theta_1$ , i.e., on the "adjustment angle" of the deflector. (We mean that frequency characteristic can be adjusted by rotation of Bragg cell around the  $[\bar{1}\bar{1}0]$  axis).

Consider Fig. 1 more carefully to analyze this dependence. Varying the angle  $\theta_1$  means that the point A travels along the curve  $|k_1(\theta)|$ , and the normal to transducer N shifts in parallel to itself. This causes that a length of vector  $\mathbf{K}_C$  and an angle  $\alpha_C$  between a tangent to the curve  $|k_2(\theta)|$  and the  $[110]$  axis are changed, i.e., depend on the angle  $\theta_1$ . Thus, the frequency  $f_C = \mathbf{K}_C(\alpha_C) \cdot v(\alpha_C) / 2\pi$  depends on the angle  $\theta_1$  in a complicated way (here  $v(\alpha_C)$  denotes a sound wave velocity traveling at the angle  $\alpha_C$  to the  $[110]$  axis). Until now, researchers following Dixon<sup>13</sup> used the condition  $\partial\theta_1/\partial f = 0$  to find the incident angle  $\theta_1$ , not taking into account that, in fact,  $\theta_1$  is a parameter. For this reason the frequency  $f_C$  and the angle  $\alpha_C$  had a special significance in the theory of non-axial deflector on  $\text{TeO}_2$ . They were usually considered as basic parameters when the deflector characteristics were analyzed. Until references 7-9 were published, the usual



way<sup>2-5</sup> was to consider interaction of the plane light wave (vector  $\mathbf{k}_1$ ) with the plane sound wave which was described exactly by vector  $\mathbf{K}_C$ . It was assumed that  $\mathbf{K}_C$  was tangent to the curve  $\mathbf{k}_2(\theta)$ , and the angle  $\alpha_C$  determined all properties of the deflector. It was assumed as well<sup>2</sup> that a bandwidth of AOI is largest in this case. Such an approach by no means took into account divergence of the sound beam. Authors of references 7-9 considering the divergent sound beam and introducing a set of calculated parameters, have proposed the calculation procedure for deflector on  $\text{TeO}_2$ . They have taken into account a change of the sound divergence when frequency was changed. Using the bounding frequencies  $f_{\min}$ ,  $f_{\max}$  and efficiency  $\eta$  as initial data, they managed to estimate basic peculiarities of the frequency characteristic and calculate  $\theta_1$ ,  $\alpha_C$ ,  $f_C$  and  $L$ . But their approach did not enable one to analyze how the frequency characteristic depended on the angle  $\theta_1$ , because  $f_C$  and  $\alpha_C$  depended on the angle  $\theta_1$  themselves.

On the other hand, the constructive angle  $\alpha_N$  between the normal to transducer N and the [110] axis is determined only by the Bragg cell construction and can not be varied after deflector fabrication (on the contrary, the angle  $\theta_1$  may be adjusted). Until now the angle  $\alpha_N$  was considered to be completely identical to the angle  $\alpha_C$ , e.g., it was assumed to be equal to  $6^\circ$ <sup>2,4,5,10</sup>. Of course, that was only valid in the special case when the normal N was tangent to the curve  $|\mathbf{k}_2(\theta)|$ , and the angle  $\theta_1$  was rigorously equal to a certain value. Thus, it is impossible to analyze the dependence of frequency characteristic on the angle  $\theta_1$ . The decision is to consider the angles  $\alpha_N$  and  $\theta_1$  as basic parameters and analyze the frequency characteristic varying them. Using the constructive parameter  $\alpha_N$  instead  $\alpha_C$  makes this possible. This approach enables one to distinguish the influence of different parameters on a frequency characteristic shape.

In real construction, the angle  $\theta_1$  is not changed after adjusting the deflector. But it is obvious

that if the angle  $\theta_1$  is fixed (i.e., the point A is tied to its place), the length of an arbitrary vector  $\mathbf{K}$  and its direction will be correlated unambiguously. In other words, the angle  $\alpha$ , determining directions of vectors  $\mathbf{K}$ , for which Bragg conditions are performed, will depend on frequency, i.e.  $\alpha = \alpha(f)$  when  $\theta_1$  is a parameter.

The dependence of Bragg angle  $\Theta$  (see, e.g., the angle  $\Theta_N$  for the wave vectors  $\mathbf{K}_{N1,2}$  in Fig. 1) vs frequency is determined by Dixon's equations (in form <sup>4</sup>):

$$\Theta(f, \alpha(f, \theta_1)) = \frac{\lambda \cdot f}{2 \cdot n_1(\theta_1) \cdot v(\alpha(f, \theta_1))} \left[ 1 + v^2(\alpha(f, \theta_1)) \frac{n_1^2(\theta_1) - n_2^2(f, \alpha(f, \theta_1))}{(\lambda \cdot f)^2} \right], \quad (1)$$

$$\text{where} \quad \theta_2(f, \alpha(f, \theta_1)) = \theta_1 + \frac{\lambda \cdot f}{n_o \cdot v(\alpha(f, \theta_1))}. \quad (2)$$

(We have written  $v = v(\alpha)$  in these equations to emphasize the strong dependence of the sound velocity on the direction of  $\mathbf{K}$  near the [110] axis in  $\text{TeO}_2$ .) Here  $\lambda$  is the light wavelength in vacuum,  $n_1(\theta_1)$  and  $n_2(\theta_2)$  are indexes of refraction for incident and diffracted light beams accordingly,  $n_o$  is an index of refraction for an ordinary beam. Substituting (2) into (1) and taking into account that  $\alpha = \Theta + \theta_1$  yields, after the performing the required algebra, a functional equation with regard to  $\alpha(f, \theta_1)$ :

$$\alpha(f, \theta_1) - \theta_2(f, \alpha(f)) = \Theta(f, \alpha(f, \theta_1)) - \frac{\lambda \cdot f}{n_o \cdot v(\alpha(f, \theta_1))}. \quad (3)$$

Now one can find  $\alpha(f, \theta_1)$  solving equation (3) and then calculate frequency characteristic, but it seems to be rather complicated. We use another procedure instead considering couple of numerical arrays  $\alpha_j, f_j$  and constructing numerical function  $\alpha(f)$  with  $\theta_1$  as a parameter. This procedure is described completely in the appendix.

If the transmission losses  $TL$  of electro-acoustic transducer are not dependent on frequency, the acoustic power  $P_a$  of the plane sound wave interacting with the plane incident light wave will

only depend on the difference  $\Delta\alpha = \alpha - \alpha_N$ . The efficiency of the acousto-optical interaction in that case

$$\eta_0(f, \Delta\alpha) = \sin^2 \left[ \frac{\pi L}{\lambda \cos(\Theta(f))} \sqrt{\frac{M_2 P_a}{2LH}} \cdot F(f, \Delta\alpha) \right], \quad (4)$$

where  $\Theta(f) = \alpha(f) - \theta_1$ , and

$$F(f, \Delta\alpha) = \frac{\sin(\pi X(f, \Delta\alpha))}{\pi X(f, \Delta\alpha)}, \quad X(f, \Delta\alpha) = \frac{L \cdot \Delta\alpha \cdot f}{v}, \quad (5)$$

are functions reflecting an influence of the transducer pattern in the plane of interaction, and  $M_2$  is a figure of merit. But the dependence  $\alpha(f)$  is already calculated, and replacing  $\Delta\alpha$  into  $\Delta\alpha(f)$  and  $v$  into  $v(\alpha(f))$  in (4), & (5) yields the frequency characteristic  $\eta_0(f)$  describing efficiency of AOI inside the crystal. To take into account the reduction of efficiency because of changing the polarization state, it is enough to use equations <sup>14</sup>

$$I_r(\theta) = \frac{1}{1 + \xi^2(\theta)} \cdot I_0, \quad \xi(\theta) = \frac{\Delta n_a(\theta)}{\Delta n_b(\theta) + \sqrt{\Delta n_b^2(\theta) + \Delta n_a^2(\theta)}},$$

$$\Delta n_a(\theta) = (n_1(0) - n_2(0)) \cdot \cos^2 \theta, \quad \Delta n_b(\theta) = (n_e(0) - n_o(0)) \cdot \sin^2 \theta \quad (6)$$

where  $I_0$  is the intensity of the input linearly polarized light, i.e., the incident light out the crystal,  $\xi(\theta)$  is ellipticity of the elliptically polarized light with intensity  $I_r(\theta)$  in  $\text{TeO}_2$ . Thus the “ultimate” frequency characteristic depending on parameters  $\alpha_N$  and  $\theta_1$  is

$$\eta(f, \alpha_N, \theta_1, P_a) = \eta_0(f, \alpha_N, \theta_1, P_a) \cdot I_r(\theta_1) / I_0. \quad (7)$$

Now, one can analyze it using acoustic power  $P_a$ , constructive parameters  $\alpha_N$ ,  $L$ ,  $H$  and the adjustment parameter  $\theta_1$  as initial data. The entire frequency characteristic will be obtained as a result.

Such an analysis has been completed for deflectors at  $\lambda=633$  nm and 514 nm. The results are presented below, (note here that there was no need to take into account a midband degeneracy in the frequency range considered <sup>9</sup>).

We used the  $\text{TeO}_2$  material constants in calculations as follows<sup>1, 4, 14, 15</sup>. Density,  $\text{kg/m}^3$ ,  $\rho = 5990$ ; Elastic stiffness constants,  $\text{Newton/m}^2$ ,  $c_{11} = 5.57 \cdot 10^{10}$ ,  $c_{12} = 5.12 \cdot 10^{10}$ ,  $c_{44} = 2.65 \cdot 10^{10}$ ; Specific optical rotation,  $\text{deg/m}$ ,  $R = 87 \cdot 10^3$  ( $\lambda = 633 \text{ nm}$ ), and  $R = 157 \cdot 10^3$  ( $514 \text{ nm}$ ); Indexes of refraction  $n_o = 2.2597$  ( $633 \text{ nm}$ ),  $n_o = 2.312$  ( $514 \text{ nm}$ ),  $n_e = 2.4119$  ( $633 \text{ nm}$ )  $n_e = 2.474$  ( $514 \text{ nm}$ );

The figure of merit for the linearly polarized light was assumed to be equal to  $M_2 = 700 \cdot 10^{-15} \text{ sec}^3/\text{kg}$ . Its measured value near the  $[001]$  is equal to  $800\text{-}1000$ <sup>14</sup>, but we used a lesser value to provide some reserve in the calculated efficiency when  $\theta_1$  does not vanish, (of course  $M_2$  would have been calculated exactly for the certain  $\theta_1$  value if all components of the photoelastic tensor had been known exactly, but different sources give differences up to 50%).

Fig. 2 represents the general shape of the frequency characteristic calculated within the range 30-140 MHz when the transducer pattern orientation is similar to that shown in Fig. 1. There are three curves: 1 - the "ultimate" frequency characteristic  $\eta(f)$ . It takes into account the reduction of efficiency due to the changing of incident light polarization<sup>14</sup> when it is propagating at an angle  $\theta_1$  from the  $[001]$  axis; 2 - frequency characteristic without that effect  $\eta_0(f)$ . Comparing curves 1 and 2 one can see the reduction of efficiency caused by the effect mentioned above; 3 - the frequency characteristic under very small efficiency  $F(f)$  normalized to unity.

In fact, curve 3 is an image of the transducer "dynamic" far-field pattern. The pattern is changed itself when frequency is changed. There is no interaction when the angle  $\alpha(f) < \alpha_C$ , and efficiency is determined by a difference  $\Delta\alpha = \alpha - \alpha_N$ . If the transducer pattern is located as it is shown in Fig. 1, the maximal efficiency  $\eta_{\max}$  is obtained at two frequencies  $f_{\text{peak1}}$  and  $f_{\text{peak2}}$  (vectors  $\mathbf{K}_{N1}$  and  $\mathbf{K}_{N2}$ ). The dip (note, it is not because of midband degeneracy<sup>1</sup>) at frequency  $f=f_M$  disappears when  $\alpha_N = \alpha_C$ , but only half of the pattern "works" then causing reduction of bandwidth.

The frequency characteristic in this case always images only a part of a pattern, which is located below vector  $\mathbf{K}_C$ , but twice. For the first time it occurs in the low-frequency range, and for the second time in the high one. So the frequency characteristic would have appeared exactly as two mirror images relative to the vertical line traveling through the frequency  $f_C$  if the transducer pattern shape had not depended on frequency, (note here that our analysis does not take into account acoustic loss).

Figure 2 represents the optimum frequency characteristics in such a sense that a bandwidth  $\Delta f = f_{\max} - f_{\min}$  has a maximum value for a certain value of  $\eta_M = \eta(f_M)$ . It was obtained by varying the  $\theta_1$  parameter for the deflector with  $L=3$  mm,  $H=3$  mm,  $\alpha_N=6^\circ$ ,  $P_a=200$  mW. This is exactly one described in reference <sup>2</sup> but a more precise angle  $\theta_1=4.375^\circ$  provides a maximal bandwidth  $\Delta f=48.3$  MHz with  $\eta_M=0.803$  (see curve 1). The side peaks (above 100 MHz and below 30 MHz) describe AOI with side lobes of the transducer pattern. One also observes a few percent decrease in efficiency because of the incident light ellipticity (compare curves 2 and 1).

Now one can analyze how the frequency characteristic is changed when the constructive parameters and acoustic power are varied, assuming that the Bragg cell is to be used in a 2-D deflector with crossed cells. Then  $H=D$ , where  $D$  is an input light beam diameter, and resolution (by Rayleigh)  $N=H\Delta f/v(\alpha_N)$ . Further, a Bragg cell will be considered with the resolvable spot number  $N>512$ . The characteristics of such a  $6^\circ$  deflector is presented in Fig. 3 (a). Naturally it was necessary to increase  $P_a$  up to 450 mW in the calculation to save the efficiency, because  $L/H$  is only equal to 0.5 in this case. The  $P_a$  value and  $\theta_1=4.353^\circ$  gives the maximum bandwidth  $\Delta f=59.6$  MHz with the minimum efficiency, which was assumed to be  $\eta_M>0.707$ , to obtain a common efficiency of more than 0.5 for a 2-D deflector

Figure 3 (b) represents how the frequency characteristic is varied when  $P_a$  increases. The central dip goes up and almost disappears, but two other lateral dips appear in the sides (curve 1,  $P_a=800$  mW). This happens because of the nonlinear dependence of  $\eta(P_a)$ . The central dip disappears completely, when  $P_a$  goes up, but the lateral dips go down (curve 2,  $P_a=1100$  mW). They are located exactly at the frequencies  $f_{\text{peak1}}$  and  $f_{\text{peak2}}$ , i.e., at the frequencies of the maximum  $P_a$  in the transducer pattern (curve 3). Thus, when  $P_a$  goes up to some value of  $P_{\text{amax}}$  on the normal to the transducer, the efficiency  $\eta$  goes over a maximum and then decreases. At the same time, the efficiency of the light interaction with the less power sound wave in the center of the frequency characteristic still only gets its maximum value. This effect is practically useful to get a uniform frequency characteristic, but requires an increased  $P_a$  to use it.

Now consider what happens if the  $\theta_1$  value is slightly different from appointed, i.e. the deflector adjustment is not performed precisely. (Note here that the  $\theta_1$  angle was calculated with precision to thousands of degree.) In Fig. 4 two such cases are shown. It is seen that very small changes in  $\theta_1$  (a few hundredth of degree) cause considerable changes in  $\eta(f)$ . The case when the transducer pattern is "looked through" by the light beam almost completely twice is presented by curve 1. It is observed in the experiment as a bifurcation of a light line produced by the scanning beam on the screen. Such an adjustment means that the normal to transducer N is located far from a tangent to the curve  $|k_2(\theta)|$ . The second case (curve 2) gives a short bright line. This is just a case, described above, when half of a transducer pattern works and the normal N is located on a tangent, i.e., the case which was usually analyzed<sup>2,5,11</sup> as to be necessary to obtain maximum bandwidth. One can see however, that that is not optimal for this purpose. From the analysis done above, it becomes obvious as well the cause for getting the rectangular frequency characteristic shape observed by many authors<sup>2,4,10,11</sup> when the incident angle  $\theta_1$  is slightly

different from calculated one. Actually, their approach used for  $\theta_1$  calculation is just the last analyzed case. Thus by slightly decreasing  $\theta_1$ , they obtained the result described.

### Optimal deflector design

One can not make an effective design without first being aware of the basic constructive parameters affecting deflector performance and understanding their effects. So we need to formulate some criteria of optimal design and define corresponding procedures. (Note here that optimal design means to chose constructive parameters of Bragg cell and “to put” the main lobe of a transducer pattern onto curves  $|k_2(\theta)|$  and  $|k_1(\theta)|$  in the best way). From an analysis made above, it follows that such criteria can not be universal ones and an attempt to minimize  $P_{dr}$  without taking into account the other deflector parameters seems to be unreasonable. Yet it can be made, if one assumes only a few basic parameters. They may be  $\eta_M$ ,  $N$ , and  $\Delta f$ .

Assume for example,  $\eta_M > 0.707$ ,  $N > 512$ ,  $\Delta f > 40$  MHz. Now varying  $L$ ,  $H$ ,  $\alpha_N$ ,  $P_a$  and making a precision adjustment of  $\theta_1$  to get the required parameters, a suitable deflector construction can be found. The acoustic power can be considered in that case as a result.

Results of such a procedure for  $6^\circ$  and  $5.5^\circ$  deflectors are represented in Fig. 5 and 6. Here (in figures)  $f_{tr} = \sqrt{f_{min} \cdot f_{max}}$  is an operating frequency of the electro-acoustic transducer and  $\Delta f_{tr} = (f_{max} - f_{min})/f_{tr}$  is its required relative bandwidth.

Consider the obtained data more carefully. Inspection of the calculation results for different constructive versions of deflectors with the same angle  $\alpha_N$  and similar performances (Fig. 5, curve 1 and 2) indicates that generally speaking,  $\theta_1$  and  $f_{tr}$  depend on  $L$ , but the last dependence is not strong. However, the relative bandwidth of the transducer is essentially greater in case 1, when  $L$  is less. On the other hand, its surface  $S=L \times H$  is almost half the size in that case; therefore, from

the point of view of the electro-acoustic efficiency, it can not be said unambiguously which case is better. The ultimate conclusion can be made only after experimental examining of a designed deflector.

The frequency characteristic of the  $6^\circ$  deflector with a usual transducer (curve 1 in Fig. 5,  $L = 3$  mm) indicates as well that apparently  $P_a$  may be reduced by loosing in bandwidth  $\Delta f$ , which is much greater than 40 MHz.

It is also seen that the  $6^\circ$  deflector with  $L = 5$  mm (curve 2) is an almost optimum one in the mentioned sense, but there is still some reserve in the bandwidth which can be used to reduce  $P_{dr}$  further. Results of such an attempt are represented in Fig. 6 (curve 1). The given requirements are practically completely obtained by construction of the  $5.5^\circ$ . Actually, acoustic power  $P_a = 320$  mW is the lowest, and other parameters are suitable too. Besides, further reduction of  $P_a$  is not merely possible because of unacceptable deterioration of other parameters.

Fig. 6 (curve 2) also shows an efficiency characteristic of the  $5.5^\circ$  deflector at  $\lambda = 514$  nm, designed from the same criteria. It is located in a much higher frequency range. It means that the same optimal deflector can not be used for the different wavelengths provided the super-wide-band transducer is used. But, in this case the transducer efficiency certainly has to be less.

Note that in fact, an iterative process has been used to obtain the required frequency characteristic at  $\lambda = 633$  nm. At first, some angle  $\alpha_N < 6^\circ$  and length of interaction were chosen, then the frequency characteristic and its bandwidth  $\Delta f$  were calculated. The angle  $\theta_1$  was varied at some reasonable  $P_a$  value, and at last the height of interaction  $H$  to obtain  $N > 512$  at the  $\Delta f$  was chosen. Finally,  $\theta_1$  and  $P_a$  values were found precisely. Probably the same process for  $\lambda = 514$  nm could lead to a better result with another  $\alpha_N$ , e.g. in case of  $\alpha_N = 5^\circ$  or  $6^\circ$ .

### **Experimental investigations of the $5.5^\circ$ deflector**



The frequency characteristics  $\eta(f)$  at different drive power levels were measured using the experimental setup shown in Fig. 7. It consisted of the connected electrical and optical parts. The electrical part included the deflector driver, the universal I/O interface, the radio-frequency counter, and the power meter. The driver and the I/O interface have been located inside the PC. The power meter and the counter were standard instruments that were connected to the computer through the I/O interface.

The deflector drive power was measured indirectly. We imply here the drive power as an available power of the drive signal source, i.e., the power that the generator can give out into the matched load. In that case  $P_{dr}$  can be measured independently, and different deflectors can be compared working with different drivers. Thus, the  $P_{dr}$  value was determined as an output power of a signal source (a driver or a generator), which drove a deflector to provide special characteristics.

The driver had output power up to 900 mW within the frequency range 40 - 90 MHz. Its output impedance was not measured; therefore, it was necessary to use the external attenuator. The 3 or 6 dB value attenuators have been used. The uniformity of the output  $P_{dr}(f)$  characteristic within the  $\pm 0.5$  dB was provided with the special calibrating procedure. It consisted in the measuring of the output power at the 32 fixed frequencies and controlling by power until its given value had been achieved. While this procedure was carried out, the driver output was connected to the power meter, not to the deflector.

The power meter input impedance was equal to 50 ohm as were all the cables used. Thus, the  $P_{dr}$  value measurements with the 50 ohm feeder have been performed. The precision of the power meter itself was within  $\pm 8$  %.

The optical part was mounted on an optical bench. The linearly polarized He-Ne laser was setup in a way to allow rotation around its axis, changing the electrical vector  $\mathbf{E}$  orientation in the incident light beam.

An experimental sample at  $\lambda=633$  nm was fabricated from a single crystal of  $\text{TeO}_2$  with common sizes  $26 \times 25 \times 13$  mm<sup>3</sup> and the constructive parameters are given in Fig. 8. Its optical surfaces were covered by  $\text{SiO}_2$  antireflection coating. In this construction, the incident outside angle  $i$  is equal to the constructive angle  $\beta$ , which can be calculated from the obvious equation

$$\arcsin[n_1(\theta_1) \cdot \sin(\beta + \theta_1 - \alpha_N)] - \beta = 0 \quad (8)$$

to provide an output angle  $\theta_{\text{out}}(f) = \arcsin[n_2(\theta_2(f)) \cdot \sin(\theta_2(f) - \alpha_N)]$  equal to 0 at some central frequency within operating range when  $\theta_2 = \alpha_N$ . The constructive angles were fabricated within  $\pm 5$  angle second. The shear-wave transducer was fabricated from the  $163^\circ$   $\text{LiNbO}_3$  plate that was bonded to the  $\text{TeO}_2$  element by means of the vacuum diffusion welding, and then was ground up to the required thickness.

According to the results obtained in the numerical simulation above, the examined deflector had the angle  $\alpha_N$  equal to  $5.5^\circ$ . Its transducer with operating frequency  $f_{\text{tr}}=55.8$  MHz had a surface  $S=6(L) \times 8$  mm<sup>2</sup> and had been matched by means of the third order transformerless optimal matching network<sup>16</sup>. Measured and calculated dependencies of voltage standing wave ratio ("VSWR") vs frequency are represented in Fig. 9. Curve 1 is the calculated VSWR of the matched transducer, but not the VSWR of the equivalent circuit. It has been calculated as an input VSWR of the matching network loaded by the transducer input impedance found experimentally. The difference between input impedances of the transducer and its equivalent circuit causes the distortion of the frequency characteristic compared with the ideal Tchebysheff one. The calculated

matched bandwidth  $\Delta f_{\text{mch}} = 29.4$  MHz (40.4-69.8 MHz,  $VSWR_{\text{max}} = 2.41$ ) has been obtained with this transducer instead of the expected 40 MHz value. Curve 2 is the measured  $VSWR$  of the real matching network constructed as a lumped one. The maximal  $VSWR$  level within the matched bandwidth  $\Delta f_{\text{mch}} = 32.3$  MHz (39.8 - 72.1 MHz) was equal to 2.51.

We note here that the measured quality factor  $Q=5.21$  appeared to be unexpectedly large. Thus, this large value of  $Q$  together with rather low operating frequency  $f_{\text{tr}}=55.8$  MHz were the reasons prevented attainment of the expected bandwidth.

The Bragg cell was mounted so as to provide a precise rotation around two perpendicular axes. The precision adjustment around the main axis allowing adjustment of the angle  $\theta_{\text{adj}} \approx \theta_1 \cdot n_1(\theta_1)$  was within  $\pm 9$  angle seconds. The laser beam was expanded by the telescope and then was limited by an aperture (diaphragm) 8 mm in diameter. The linearity of the photodiode was provided by the red optical filter with the necessary attenuation located before it. The measured frequency characteristic  $\eta(f)$  was imaged on the computer display and was recorded into the disk. Typical displayed images are represented below.

As was mentioned above, there is a maximum acoustic power level that when exceeded gives an efficiency decrease. The corresponding drive power  $P_{\text{dmax}}$  level was found to be about 410 mW. Therefore the  $\eta(f)$  characteristics at various  $\theta_{\text{adj}}$  have been measured while the calibrated  $P_{\text{dr}}$  was equal to 400 mW. They are presented in Fig. 10. The best characteristic (curve 2) obtained with some angle  $\theta_{\text{adj}} = \theta_{\text{adj0}}$  provided a deflector bandwidth of  $\Delta f = 27.1$  MHz (44.2 - 71.3 MHz) at the level  $\eta_M = 0.45$  with maximum efficiency  $\eta_{\text{max}} = 0.68$ . The high bounding frequency  $f_{\text{max}} = 71.3$  MHz was determined by the transducer band, but the low bounding frequency  $f_{\text{min}} = 44.2$  MHz was apparently limited by the transducer pattern width. Note that there is a peak efficiency at the frequency of  $f_{\text{peak1}} = 49.6$  MHz described above (see Fig. 2 as well), but it is absent in the high-

frequency part of the characteristic curve. Two other device characteristics were obtained for  $\theta_{adj}$  varying by  $\pm 3'$ . Curve 1 represents the case when the pattern of the transducer is "looked through" twice by the light wave. The low-frequency peak is well observed, but the high-frequency one is absent because of the limited transducer bandwidth. Curve 3 represents the case when only half of the transducer pattern works. Differences between the calculated and measured characteristics are discussed below.

Figure 11 shows the behavior of the  $\eta(f)$  characteristic when the drive power is changed. The  $P_{dr}$  values were 200, 400, 600 mW and the adjustment angle  $\theta_{adj}$  was equal to  $\theta_{adj0}$ . As mentioned, the output power of the driver was limited by the value 900 mW; therefore, the external attenuator can not be used in the last case. Owing to this reason, the efficiency characteristic obtained at 600 mW has an illustrative significance. The effect of the deterioration of the essential efficiency characteristic when  $P_{dr} > P_{drmax}$  is clearly observed. It occurs already at the  $P_{dr} = 600$  mW (curve 3). It is also seen that the  $P_{dr}$  value equal to 400 mW is close to the best one for the examined deflector. Actually, an increase in drive power up to 600 mW does not cause an increased  $\eta_{max}$ , and the bandwidth  $\Delta f$  increases only from 27.1 to 29.4 MHz in that case.

Measurements of  $7.9^\circ$  Bragg cell characteristics with an operating frequency  $f_{tr} = 85$  MHz have been performed (see Fig.12) to compare drive power reduction in the  $5.5^\circ$  device in spite of the limited driver maximum frequency of 90 MHz. In this case, even  $P_{dr} = 800$  mW was less than  $P_{drmax} \approx 980$  mW at  $f = 73$  MHz, which was measured using an additional generator. Note as well that the  $\eta_{max}$  value of the  $7.9^\circ$  deflector was less than the  $\eta_{max}$  value of the  $5.5^\circ$  deflector (0.60 and 0.68 correspondingly).

## Discussion of Results

In spite of a good qualitative agreement between measured and calculated frequency characteristics, quantitatively they are strongly different. First of all, the experimentally obtained efficiency is much less than the calculated one. Moreover, we could not obtain improved efficiency by increasing the drive power. Apparently it can be caused by an acoustic loss which has not been taken into account in the model used. Actually, in the case of an arbitrary acoustic power the normalized efficiency of light diffracted under Bragg angle <sup>17</sup>

$$\zeta = \frac{1}{D} \int_0^D \sin^2 \left[ \frac{\pi \cdot P}{2} \exp(-\alpha z) \right] dz, \quad (9)$$

$$\text{where} \quad P = qL/\pi, \quad q = \frac{\pi}{\lambda \cdot \cos \Theta} \sqrt{\frac{M_2 \cdot P_a}{L \cdot H}}, \quad (10)$$

$\alpha$  is the acoustic loss factor. Assuming that  $\alpha$  is directly proportional to  $f$ -square and using the acoustic loss value equal to  $16 \text{ dB} \cdot \text{sec}^{-1} \cdot \text{MHz}^{-2}$  for shear waves along the [110] axis, one can calculate the frequency dependence  $\zeta(f)$  at various levels of  $P_a$ . Note that the  $\zeta$  value depends on the constructive parameter  $H$ , not only because of (9), but also it follows from  $H = D$  in the 2-D construction as far as common acoustic loss on the aperture depends on  $H$ . Taking into account this fact, it is interesting to compare the examined deflector with the best one described in reference 2. It is the  $6^\circ$  deflector with the transducer 3 by 3 mm. Its efficiency was equal to 0.80 at the  $P_{dr} = 350 \text{ mW}$ . Using it in a 2-D construction one can obtain the resolution  $N=223$ , because of the small  $H$  value. The  $5.5^\circ$  cell provides  $N=337$  even at the obtained  $\Delta f = 27.1 \text{ MHz}$ , but its maximum efficiency is equal only to 0.68. Thus, it is necessary to perform additional investigations to find the actual optimum construction.

Curves calculated using (9) are represented in Fig. 13. Curve 1 describes the  $6^\circ$  deflector<sup>2</sup>. One can see a good agreement with this curve and experimental results<sup>2</sup>. The  $P_a$  value equal to 320 mW for the  $5.5^\circ$  device (curve 2) was chosen from the calculation done above (see Fig. 6). The  $L$  and  $H$  values were chosen in a similar manner. Significant efficiency reduction is observed as well. Note that the higher efficiency of the  $6^\circ$  deflector compared with the  $5.5^\circ$  deflector is observed because of the higher  $H$  value in the second case (8 mm against 3 mm). Thus, less efficiency is a payment for saving the given  $N > 512$  value in 2-D construction. The  $P_a$  value equal to 700 mW (curve 3) for the  $7.9^\circ$  Bragg cell was used assuming that the best  $P_{dr}$  value is about 900 - 950 mW and the transmission loss of the transducer is approximately equal to the transducer loss of the  $5.5^\circ$  deflector.

Experiment confirmed the strong dependence of the  $\eta(f)$  characteristic on the angle  $\theta_{adj}$  as well. At the same time, the essential difference in the entire characteristic shape is observed for calculated and measured curves, and if the lack of a high frequency peak on curve 1 can be explained from the limited transducer bandwidth, the behavior of the measured characteristics in the domain A (see Fig. 10) has no reasonable explanation. Actually, the peak on curve 2 is not observed and there is even a slope in this place on curve 3. The efficiency reduction in the last case compared with curves 1 and 2 is also not explained. Perhaps some of these differences are caused by the transducer pattern distortion because of non-uniform sound field distribution.

## Conclusions

From the obtained results one can make following conclusions.

- (1) In  $\text{TeO}_2$ , parameters of the usually used physical model  $\alpha_c, f_c$  depend only on the parameter  $\theta_1$  (the angle between  $[001]$  and the incident light wave vector) if the AO interaction occurs in the

( $\bar{1}10$ ) plane. (2) Using an additional constructive parameter  $\alpha_N$  (the angle between  $[001]$  and the normal to transducer) in this model, one can analyze the efficiency frequency dependence  $\eta(f)$  on the different factors separately. It is impossible if only the usual parameters of the physical model  $\alpha_C$  and  $f_C$  are used. (3) One ought not use bounding frequencies as initial data if an optimal design is to be made. Only the bandwidth of the deflector has to be given. (4) The true optimal design may be made only for a given light wavelength. The same Bragg cell can not be optimal for different  $\lambda$ . (5) The physical model used correctly describes the main peculiarities of the frequency characteristic, but some effects observed experimentally can not be explained in its frame. There is no reasonable explanation for the characteristic distortion in the high-frequency domain. (6) The design approach used allows one to obtain the optimum essential reduction of the drive power. At least  $P_{dr}=400$  mW per channel can be achieved for 2-D Bragg cell construction with a bandwidth of about 30 MHz and resolution more than 512 at  $\lambda=633$  nm. The  $5.5^\circ$  deflector is suitable for this purpose.

#### Appendix. Calculation of Bragg cell frequency characteristic

The dependence of the sound velocity  $v$  on the angle  $\alpha$  between the arbitrary sound wave vector  $\mathbf{K}$  and the  $[110]$  axis (Fig. A1) is described by<sup>9</sup>

$$v(\alpha) = \sqrt{\frac{1}{\rho} \cdot \left( \frac{c_{11} - c_{12}}{2} \cdot \cos^2 \alpha + c_{44} \cdot \sin^2 \alpha \right)}. \quad (\text{A1})$$

In turn, the dependence of the indexes of refraction  $n_1$  (slow wave) and  $n_2$  (fast wave) on the angle  $\theta$  between the light wave vector  $\mathbf{k}$  and the  $[001]$  axis are<sup>9</sup>

$$n_1(\theta) = n_{01}(\theta) + \frac{1}{2} \cdot n_{01}^3(\theta) \cdot \rho(\theta) \cdot G(\theta), \quad n_2(\theta) = n_{02}(\theta) - \frac{1}{2} \cdot n_{02}^3(\theta) \cdot \rho(\theta) \cdot G(\theta). \quad (\text{A2})$$

$$\text{Here } G(\theta) = \frac{R \cdot \lambda \cdot \cos^2 \theta}{\pi \cdot n_o^3}, \quad n_{01}(\theta) = \frac{n_e \cdot n_o}{\sqrt{n_e^2 \cdot \cos^2 \theta + n_o^2 \cdot \sin^2 \theta}}, \quad n_{02}(\theta) = n_o,$$

$$\rho(\theta) = \frac{\sqrt{(n_o^{-2} - n_{01}^{-2}(\theta))^2 + (2 \cdot G(\theta))^2} - (n_o^{-2} - n_{01}^{-2}(\theta))}{2 \cdot G(\theta)}.$$

The lengths of the sound wave vectors are equal to the lengths of segments AB, AC and AD in Fig. A1. The equations for lines  $P(\theta)$  (the tangent) and  $P_{\text{sec}}(\theta)$  (the secant) in polar coordinates can be easily written from the triangles ACO, APO and AC'O, AP'O as the lengths of the segments OP and OP'

$$P(\theta, \alpha_c) = n_2(\alpha_c) \cdot \cos^{-1}(\alpha_c - \theta), \quad (\text{A3})$$

$$P_{\text{sec}}(\theta, \alpha) = n_1(\theta_1) \cdot \cos(\alpha - \theta_1) \cdot \cos^{-1}(\alpha - \theta). \quad (\text{A4})$$

As it is seen from Fig. A1, the location of the point A on the curve  $n_1(\theta)$  unambiguously determines the location of the tangent  $P(\theta)$  and the couple of values  $\alpha_c$  and  $\theta_1$ . The condition  $OA=OP$  at  $\theta=\theta_1$  and equation (A3) immediately yields an equation to establish a connection between  $\alpha_c$  and  $\theta_1$

$$n_1(\theta_1) - P(\theta_1, \alpha_c) = 0. \quad (\text{A5})$$

Given the array of the  $\alpha_{cj}$  values, the array of the  $\theta_{1j}$  values can be found as solutions of equation (A3). Then the lengths of segments  $AC_j = |K(\alpha_{cj})|$  can be calculated from the triangle ACO, and the array of the  $f_{cj}$  values from the known  $K(\alpha_{cj})$  and the equation

$$f_{cj} = v(\alpha_{cj}) \cdot \lambda^{-1} \cdot n_2(\alpha_{cj}) \cdot \tan(\alpha_{cj} - \theta_{1j}). \quad (\text{A6})$$



Now having coupled arrays  $\alpha_{Cj}$ ,  $\theta_{1j}$ , and  $\alpha_{Cj}$ ,  $f_{Cj}$ , there is a possibility to calculate numerical functions  $\alpha_C(\theta_1)$  and  $f_C(\theta_1)$  using interpolation by cubic splines. This procedure has been made by means of the MATHCAD 5.0 PLUS<sup>18</sup> application.

The numerical functions  $\alpha(f)$  and  $\theta_2(f)$  can be calculated in the same way using the equation

$$n_2(\theta_B) - P_{\text{sec}}(\theta_B, \alpha) = 0 \quad (\text{A7})$$

to find the array of  $\theta_{Bj}$  values. The array of  $f_{\text{low}j}$  values was found from the triangle AEO:

$$f_{\text{low}j} = \nu(\alpha_j) \cdot \lambda^{-1} \cdot \sqrt{n_1^2(\theta_1) + n_2^2(\theta_{Bj}) - 2 \cdot n_1(\theta_1) \cdot n_2(\theta_{Bj}) \cdot \cos(\theta_{Bj} - \theta_1)} \quad (\text{A8})$$

Here  $f_{\text{low}}$  denotes the low-frequency range  $f \leq f_C$ . The frequencies  $f_{\text{high}}$  from the high-frequency range  $f > f_C$  were calculated by replacing  $\theta_B$  into  $\theta_D$  in equations (A7), (A8) and making the same calculations. The coupling of the  $\alpha_j$ ,  $f_{\text{low}j}$ , and  $\alpha_j$ ,  $f_{\text{high}j}$  arrays yielded numerical functions  $\alpha(f_{\text{low}})$  and  $\alpha(f_{\text{high}})$  which then have been unified into one function  $\alpha(f)$ . The same procedure for the  $\alpha_j$ ,  $\theta_{Bj}$ ,  $\alpha_j$ ,  $\theta_{Dj}$  and  $\alpha_j$ ,  $\theta_{Ej}$  arrays have yielded numerical functions  $\theta_2(f)$ ,  $\theta_E(f)$ .

Thus the numerical functions  $\alpha(f)$ ,  $\theta_2(f)$  and  $\theta_E(f)$ , with parameter  $\theta_1$ , were obtained as a result. This makes it possible to calculate the entire frequency characteristic  $\eta(f)$ , the degeneracy frequency  $f_{\text{dgnr}}$  and the output angles of Bragg cell  $\theta_{\text{out}}(f)$ .

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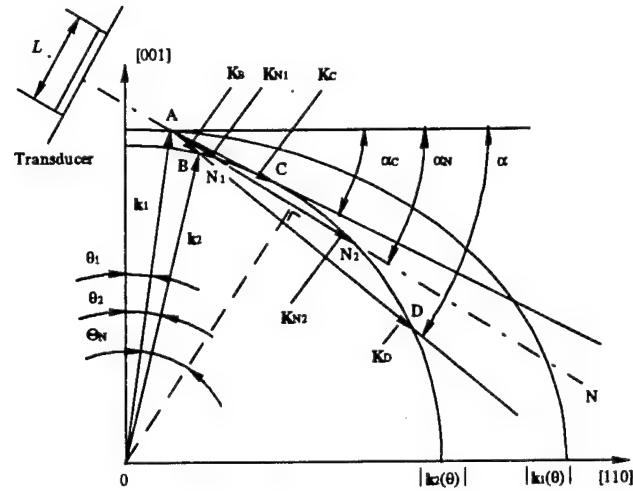


Fig. 1. The vector diagram illustrating acousto-optical interaction of the plane light wave with divergent sound beam in  $\text{TeO}_2$ .  $k_1$  - wave vector of incident light;  $k_2$  - wave vector of deflected light;  $K$  - wave vectors of sound;  $N$  - normal to the transducer;  $\theta_N$  - Bragg angle for the sound vectors lying on the normal  $N$ .

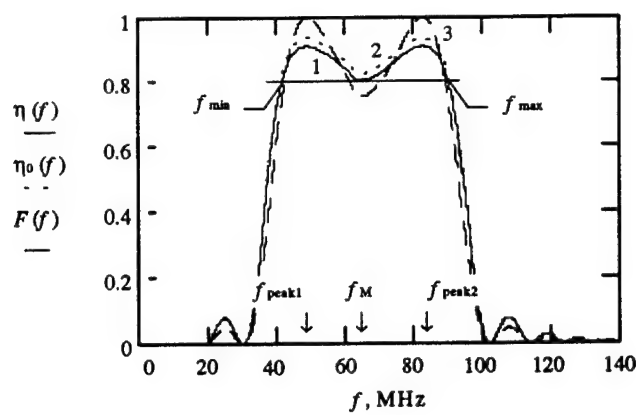
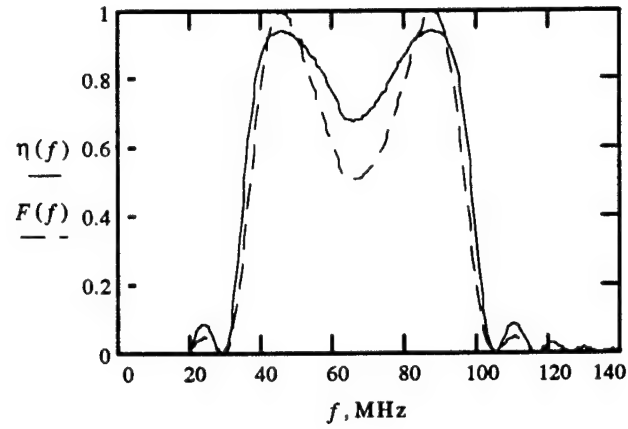
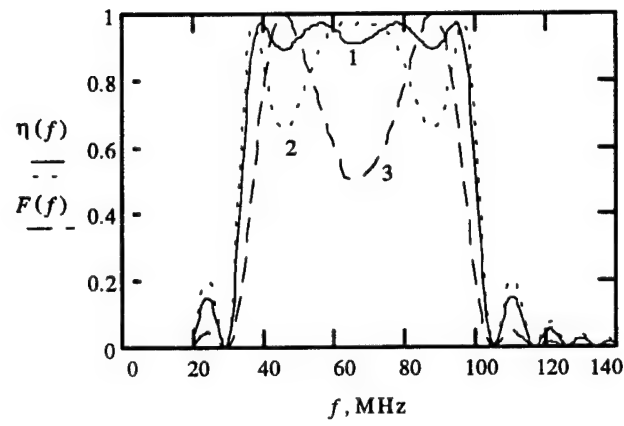


Fig. 2. Typical frequency characteristic of TeO<sub>2</sub> deflector.  $L=3$  mm,  $H=3$  mm,  $\alpha_N=6^\circ$ ,  $\theta_1=4.375^\circ$ ;  $P_a=200$  mW.



(a)



(b)

Fig. 3. Frequency characteristics of the  $6^\circ$  deflector at different  $P_a$ .

$L=3$  mm,  $H=6$  mm,  $\alpha_N=6^\circ$ ,  $\theta_1=4.353^\circ$ . (a)  $P_a=450$  mW,  $\Delta f \approx 59.6$  MHz,  $N=550$ ; (b)  $P_a=800$  mW (curve 1),  $P_a=1100$  mW (curve 2).

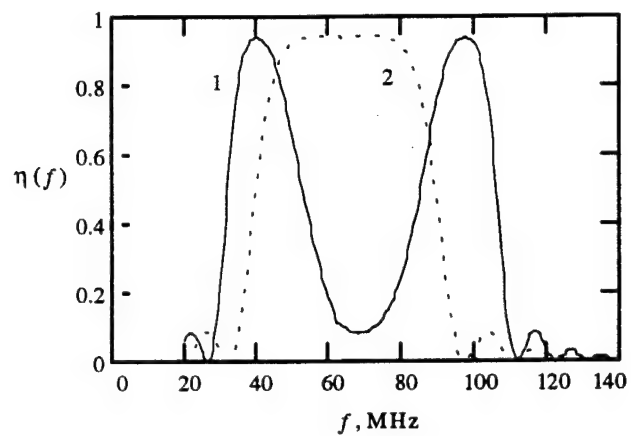


Fig. 4. Bifurcation (curve 1) and narrowing (curve 2) of frequency characteristic.

$L=3$  mm,  $H=6$  mm,  $\alpha_N=6^\circ$ ;  $P_a=450$  mW. (1)  $\theta_1=4.300^\circ$ ,  $\Delta f=80.9$  MHz,  $N=744$  ( $\eta_M<0.1$ ). (2)

$\theta_1=4.408^\circ$ ,  $\Delta f=21.3$  MHz,  $N=197$ .

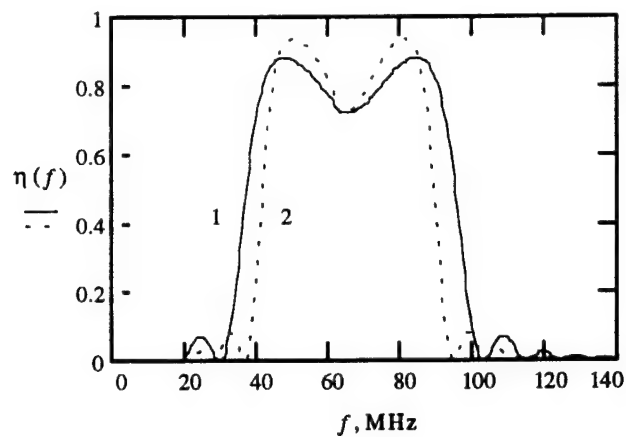


Fig. 5. Frequency characteristics of the 6° deflector at different constructive parameters.

(1)  $L=3$  mm,  $H=6.5$  mm,  $\theta_1=4.368^\circ$ ;  $P_a=400$  mW,  $\eta_M=0.722$ ,  $N=522$ ,  $\Delta f=52.1$  MHz,  $f_r=61.0$ ,  $\Delta f_r=86$  %. (2)  $L=5$  mm,  $H=8$  mm,  $\theta_1=4.382^\circ$ ;  $P_a=350$  mW,  $\eta_M=0.720$ ,  $N=543$ ,  $\Delta f=44.1$  MHz,  $f_r=61.9$ ,  $\Delta f_r=71$  %.



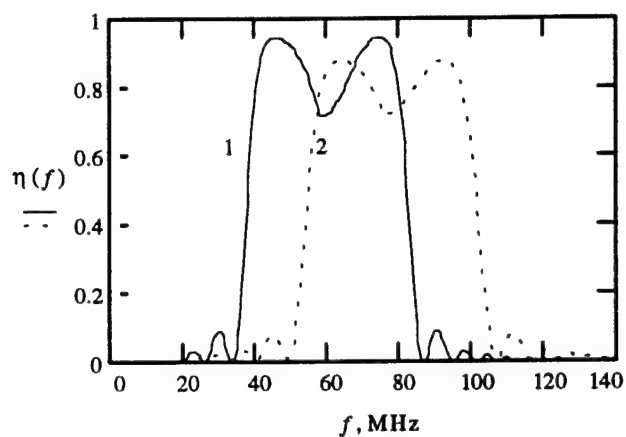


Fig. 6. Frequency characteristics of the  $5.5^\circ$  deflector at different wavelength.  $L=6$  mm,  $H=8$  mm,  $\alpha_N=5.5^\circ$ . (1)  $\lambda=633$  nm,  $P_a=320$  mW,  $\theta_1=4.004^\circ$ ;  $\eta_M=0.716$ ,  $N=512$ ,  $\Delta f=41.2$  MHz,  $f_{tr}=56.7$  MHz,  $\Delta f_{tr}=73$  %. (2)  $\lambda=514$  nm,  $P_a=180$  mW,  $\theta_1=3.963^\circ$ ;  $\eta_M=0.715$ ,  $N=519$ ,  $\Delta f=41.7$  MHz,  $f_{tr}=75.5$  MHz,  $\Delta f_{tr}=55$  %.

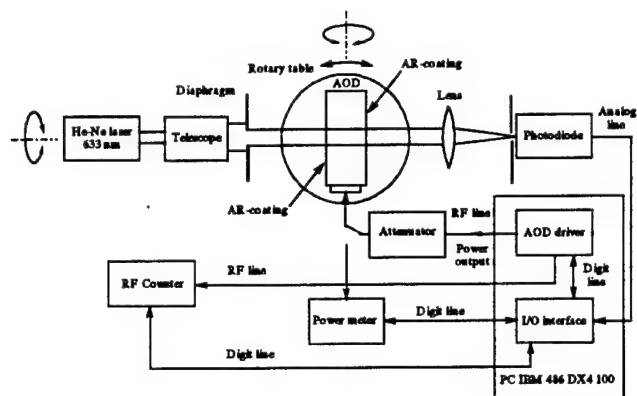


Fig. 7 Experimental setup for measuring frequency dependence of deflected light intensity.

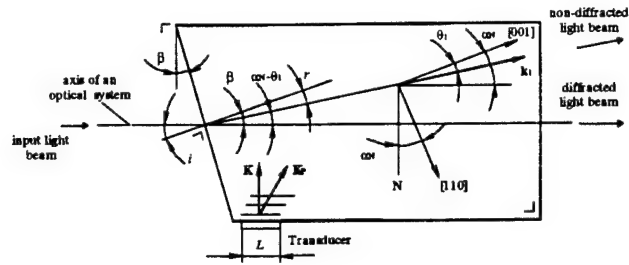


Fig. 8. Construction of Bragg cell for 2-D deflector.

$k_1$  - wave vector of incident light;  $K$  - wave vector of sound;  $K_P$  - Poynting's vector of sound;  $N$  - normal to the transducer.

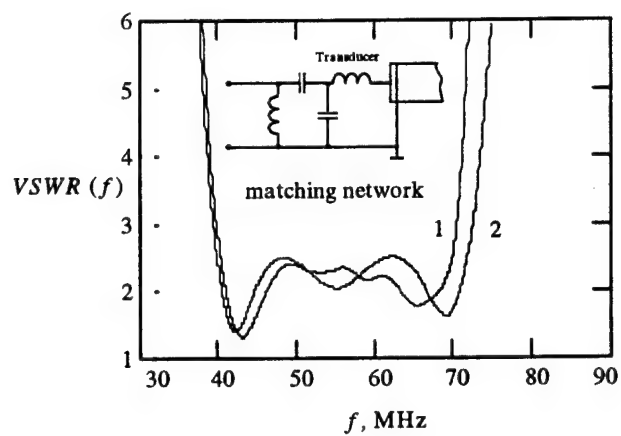


Fig. 9 Frequency dependencies of the input VSWR of the  $5.5^\circ$  deflector with an optimal matching network (1 - calculated, 2 - measured).

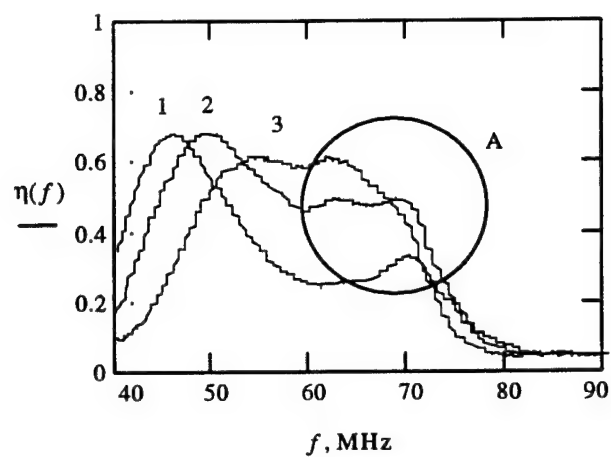


Fig. 10 Dependence of the 5.5° deflector frequency characteristic on the adjustment angle  $\theta_{adj}$ .

$P_{dr}=400$  mW;  $\theta_{adj}=\theta_{adj0}-3'$  (1);  $\theta_{adj}=\theta_{adj0}$  (2);  $\theta_{adj}=\theta_{adj0}+3'$  (3).

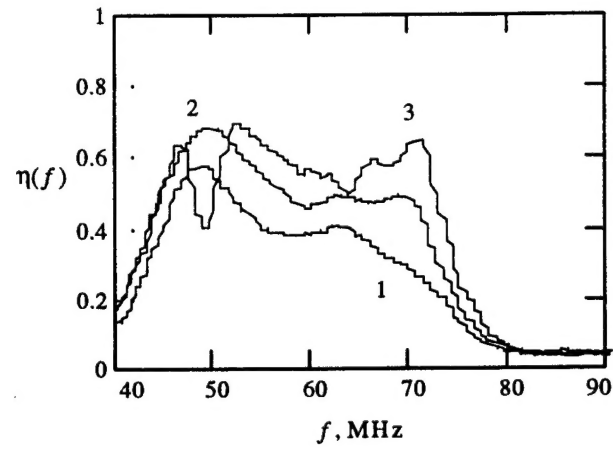


Fig. 11 Dependence of the 5.5° deflector frequency characteristic on the drive power  $P_{dr}$ .

$\theta_{adj} = \theta_{adj0}$ ;  $P_{dr} = 200$  mW (1);  $P_{dr} = 400$  mW (2);  $P_{dr} = 600$  mW (3).

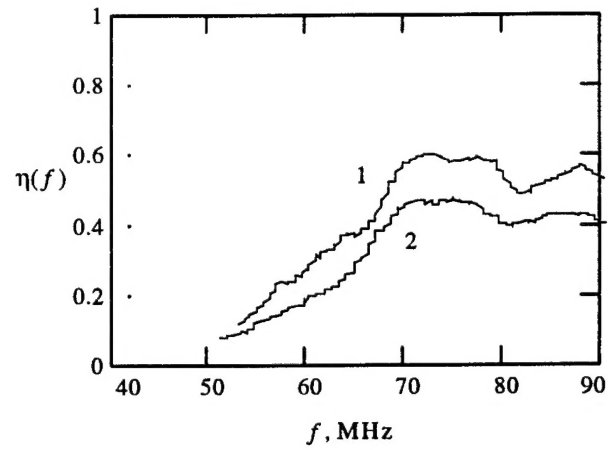


Fig. 12 Dependence of the 7.9° deflector frequency characteristic on the drive power  $P_{dr}$ .

$P_{dr} = 800$  mW (1);  $P_{dr} = 400$  mW (2).

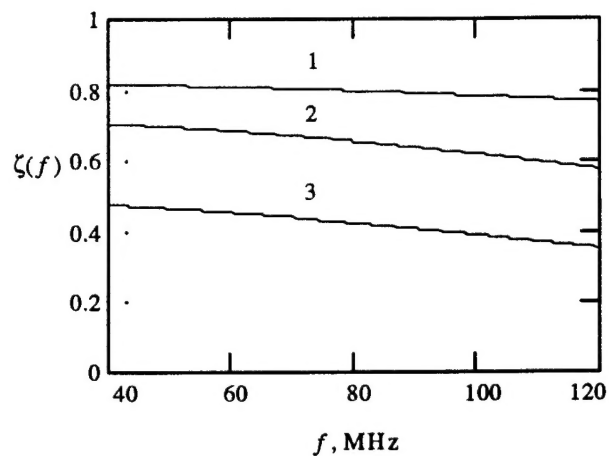


Fig. 13 Normalized intensity vs frequency of light diffracted under Bragg angle at different constructive parameters and drive power.  $\alpha_N=6^\circ$ ,  $P_a=300$  mW,  $L=3$  mm,  $H=3$  mm (1);  $\alpha_N=5.5^\circ$ ,  $P_a=320$  mW,  $L=6$  mm,  $H=8$  mm (2);  $\alpha_N=7.9^\circ$ ,  $P_a=700$  mW,  $L=2$  mm,  $H=10$  mm (3).



